

Returns and Risk

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Chapter-4 RETURN AND RISK

* Investment Return

It is the additional income generated by the investment. It is generally expressed in the form of percentage and measured on after tax basis. Return expressed in the form of percentage is called Rate of Return (r) or Holding period Return (HPR).

* Measurement of Investment Return

Generally following three types of investment returns are measured.

1. Realized Rate of Return
2. Expected Rate of Return
3. Required Rate of Return

* Realized Rate of Return

It is that return which had already been achieved or earned. It is also called past return or historical return or ex-post return and calculated by using following formula:

$$\text{HPR} = \frac{\text{Selling price} - \text{Purchase price} + \text{Dividend/Interest}}{\text{Purchase price}} \times 100$$

$$= \frac{\text{Ending value} - \text{Beginning value} + \text{Dividend}}{\text{Beginning value}} \times 100$$

where,

$$\text{Ending value} - \text{Beginning value} = \text{Capital Gain}$$

Alternatively,

$$\text{HPR} = \frac{\text{Capital Gain} + \text{Dividend}}{\text{Beginning value}} \times 100$$

$$= \frac{\text{Capital Gain}}{\text{Beginning value}} \times 100 + \frac{\text{Dividend}}{\text{Beginning value}} \times 100$$

$$= \text{Capital Gain Yield} + \text{Dividend Yield}$$

$$= \text{CGY} + \text{DY}$$

* Total Return

Total Return is the total of current income and capital gain or loss from an investment. It is calculated as follows:

$$\text{Total Rupee Return} = \text{Current income} + \text{Capital Gain (or loss)}$$

$$\text{Percentage Return} / \text{Rate of Return} = \frac{\text{Total Rupee Return}}{\text{Beginning value of Investment}}$$

Problem 4.1

Solⁿ

Beginning value = Rs. 9500

Ending value = Rs. 10,000

Interest for six months = Rs. 300

Maturity period = 18 months

a. $\text{Income} = 300 \times 3 = \text{Rs. } 900$

b. $\text{Capital Gain} = \text{Ending Value} - \text{Beginning Value}$
 $= \text{Rs. } 10,000 - \text{Rs. } 9500$
 $= \text{Rs. } 500$

c. $\text{Total Return in Rupee} = \text{Income} + \text{Capital Gain}$
 $= 900 + 500$
 $= \text{Rs. } 1400$

$$\text{Percentage Return} = \frac{\text{Total Return in Rupee}}{\text{Beginning Value}}$$
$$= \frac{1400}{9500}$$
$$= 14.74\%$$

Problem 4.2

Solⁿ

a. Calculation of total Rupee Return and percentage Return

Year	P_1	P_0	D	$CG = P_1 - P_0$	Total Rupee Return = $D + CG$	Percentage Return = $\frac{\text{Total Rs. Return}}{P_0}$
2012	220	200	10	20	30	15%
2013	230	220	20	10	30	13.64%
2014	250	230	25	20	45	19.57%
2015	280	250	40	30	70	28%
2016	350	280	20	70	90	32.14%

b. Average Rate of Return over the period 2012 - 2016

$$= \frac{15\% + 13.64\% + 19.57\% + 28\% + 32.14\%}{5}$$

$$= 21.67\%$$

c. We would expect the same average rate of return of 21.67% in 2017 if all other things remain constant.

d.

$$\text{Beginning value} = 150 \text{ shares} \times 200 = \text{Rs. } 30,000$$

$$\text{Ending value} = 150 \text{ shares} \times 250 = \text{Rs. } 37,500$$

$$\text{Dividend Income (2012-2014)} = (10 + 20 + 25) \times 150 \text{ shares} = 8250$$

$$\begin{aligned} \text{Total Return in Rupee} &= (\text{Ending value} - \text{beginning value}) + \text{Dividend} \\ &= (37,500 - 30,000) + 8250 \\ &= \text{Rs. } 15,750 \end{aligned}$$

$$\begin{aligned}\text{Rate of Return} &= \frac{\text{Total Rupee Return}}{\text{Beginning value}} \\ &= \frac{15,750}{30,000} \\ &= 52.5\%\end{aligned}$$

Problem 4.3

Solⁿ

Given:

$$\text{Real Rate of Return (K}^*) = 3\%$$

$$\text{Inflation premium (IP)} = 5\%$$

$$\text{Risk premium of A (RP}_A) = 3\%$$

$$\text{Risk premium of B (RP}_B) = 5\%$$

$$\begin{aligned}\text{a. Risk free Rate of Return (R}_f) &= K^* + IP \\ &= 3\% + 5\% \\ &= 8\%\end{aligned}$$

$$\begin{aligned}\text{b. Required Rate of Return (R)} &= R_f + RP \\ R_A &= R_f + RP_A = 8\% + 3\% = 11\%\end{aligned}$$

$$R_B = R_f + RP_B = 8\% + 5\% = 13\%$$

c. Investment B, is riskier due to higher risk premium.

Problem 4.4

Soln

a.

Bond

	A	B
Interest Received:		
First quarter	Rs. 100	Rs. 75
Second quarter	100	125
Third quarter	100	125
Fourth quarter	100	275
Total Interest Received	400	600
Investment Value:		
End of the year	Rs. 5100	Rs. 4400
Beginning of the year	5000	4500
Capital Gain or loss	100	(100)
Total Rupee Return	500	500
Holding Period Return		
HPR = Total Rupee Return	500	500
Beginning value	5000	4500
	= 10%	= 11.11%

Capital Gain or loss is not likely to be realized if we continue to hold each of the bonds beyond one year because capital gain or loss is only realized if we sell the investment.

c. Assuming both the bonds are of equal risk, we would prefer bond B because it has higher Holding period Return than bond A.

Problem 4.5

Soln

Given:

Number of shares (N) = 100 shares

Beginning price (P_0) = Rs. 20

Dividend per share (D_1) = Rs. 2

Ending price (P_1) = Rs. 21

$$\begin{aligned} \text{a. Total Rupee Return} &= [(P_1 - P_0) + D_1] \times N \\ &= [(21 - 20) + 2] \times 100 \text{ shares} \\ &= \text{Rs. 300} \end{aligned}$$

$$\text{b. HPR} = \frac{\text{Total Rupee Return}}{\text{Beginning value}} \times 100$$

$$= \frac{300}{100 \times 20} \times 100$$

$$= 15\%$$

OR

$$\text{HPR} = \frac{P_1 - P_0 + D_1}{P_0} \times 100$$

$$= \frac{21 - 20 + 2}{20} \times 100 = 15\%$$

$$\begin{aligned} \text{c. Dividend Yield} &= \frac{D_1}{P_0} \times 100 \\ &= \frac{2}{20} \times 100 \\ &= 10\% \end{aligned}$$

$$\begin{aligned} \text{Capital Gain Yield} &= \frac{P_1 - P_0}{P_0} \times 100 \\ &= \frac{21 - 20}{20} \times 100 \\ &= 5\% \end{aligned}$$

Problem 4.6

Solⁿ

	ABC	XYZ
Beginning value	Rs. 120,000	Rs. 155,000
Cash Flow (Income)	Rs. 15,000	Rs. 16,800
Ending Value	Rs. 130,000	Rs. 185,000

a. Calculation of Holding Period Return (HPR)

$$\text{HPR} = \frac{(\text{Ending value} - \text{Beginning value}) + \text{Cash flow}}{\text{Beginning value}} \times 100$$

$$\text{HPR}_{\text{ABC}} = \frac{(130,000 - 120,000) + 15,000}{120,000} \times 100 = 20.83\%$$

$$HPR_{xyz} = \frac{(185,000 - 155,000) + 16,800}{155,000} \times 100 = 30.19\%$$

b. If the two investments are equally risky, Mr. Thapa should recommend Investment XYZ because of higher return.

Problem 4.7

Soln

	Stock 1 st	Stock 2 nd
Dividend Received		
First quarter	Rs. 5	Rs. 6
Second quarter	Rs. 5	Rs. 6
Third quarter	-	Rs. 6
Fourth quarter	-	Rs. 6
Total Dividend (A)	Rs. 10	Rs. 24
Investment Value		
Beginning price	Rs. 250	Rs. 270
Ending price	Rs. 270	Rs. 300
Capital Gain (B)	Rs. 20	Rs. 30
Total Rupee Return (A+B)	Rs. 30	Rs. 54
Percentage Return (HPR)		
= $\frac{\text{Total Rupee Return}}{\text{Beginning price}}$	$\frac{30}{250} = 12\%$	$\frac{54}{270} = 20\%$
Annualized HPR	12 x 2 = 24%	-

First stock p. will provide better annualized holding period return.

Problem 4.8

Soln

	Nepal Bank LTD.	Nabil Bank LTD.	Total
Beginning value	1000 X 200 = Rs. 200,000	500 X 700 = Rs. 350,000	Rs. 550,000
Dividend in 2014	-	500 X 20 = Rs. 10,000	Rs. 10,000
Dividend in 2015	-	500 X 30 = Rs. 15,000	Rs. 15,000
Ending value	1000 X 190 = Rs. 190,000	500 X 800 = Rs. 400,000	Rs. 590,000

1. Calculation of Two-Year Holding period Return on total Investment assuming that the dividend received in 2014 was not reinvested.

$$\text{Two-Year HPR} = \frac{\text{Ending value} - \text{Beginning value} + \text{Div}_{2014} + \text{Div}_{2015}}{\text{Beginning value}} \times 100$$

$$= \frac{590,000 - 550,000 + 10,000 + 15,000}{550,000} \times 100$$

$$= 11.8\%$$

b. Calculation of Two-year holding period return, assuming that the dividend received in 2014 was reinvested at 10%.

$$\begin{aligned}\text{Two-Year HPR} &= \frac{\text{Ending value} - \text{Beginning value} + \text{Div}_{2014}(1+i) + \text{Div}_{2015}}{\text{Beginning value}} \times 100 \\ &= \frac{590,000 - 550,000 + 10,000(1+0.10)^1 + 15,000}{550,000} \times 100 \\ &= 12\%\end{aligned}$$

* Internal Rate of Return (IRR)

The annualized rate of return from an investment with more than one year of holding period, is Internal Rate of Return. IRR or Yield is a return that recognizes the concept of Time Value of money.

The internal rate of return is compared against the required rate of return to conclude on the performance of investment. If IRR is greater than or equal to the required return, the investment performance is said to be satisfactory. If IRR is lower than the required rate of return we do not accept such investment as it reduce investment wealth.

- IRR for Single cash Flow

$$FV = PV(1 + IRR)^n$$

Where,

PV = Present Value or Beginning Investment

FV = Future value or Ending value

n = Time period

Problem 4.9

Solⁿ

Given:

q.

Present value (PV) = Rs. 20,000

Future value (FV) = Rs. 40,000

Maturity period (n) = 5 Years

Internal Rate of Return (IRR) = ?

We know that,

$$FV = PV(1 + IRR)^n$$

$$40,000 = 20,000(1 + IRR)^5$$

$$IRR = \left[\frac{40,000}{20,000} \right]^{1/5} - 1$$

$$= 14.87\%$$

- b. Since, the Internal Rate of Return 14.87% is higher than the Required Rate of Return of 10%, so we would accept this offer.

Problem 4.10

Solⁿ

Given:

- a. Present value (PV) = Rs. 2500
Future value (FV) = Rs. 6000
Maturity period (n) = 8 years
Internal Rate of Return (IRR) = ?

We know that,

$$FV = PV (1 + IRR)^n$$

$$6000 = 2500 (1 + IRR)^8$$

$$\frac{6000}{2500} = (1 + IRR)^8$$

$$\left[\frac{6000}{2500} \right]^{1/8} = 1 + IRR$$

$$\% IRR = \left[\frac{6000}{2500} \right]^{1/8} - 1$$
$$= 11.56\%$$

- b. Since, the Internal Rate of Return 11.56% is higher than the required rate of return of 10%, we should make the proposed investment.

Problem 4.11

Soln

Given:

$$\text{Beginning value (CF}_0\text{)} = \text{Rs. } 7000$$

$$\text{Dividend in year 1} = \text{Rs. } 65$$

$$\text{Dividend in year 2} = \text{Rs. } 70$$

$$\text{Dividend in year 3} = \text{Rs. } 70$$

$$\text{Dividend in year 4} = \text{Rs. } 65$$

$$\text{Ending value} = \text{Rs. } 7900$$

Step-1:

$$\text{Total Return} = \text{Capital Gain} + \text{Dividend}$$

$$= (7900 - 7000) + (65 + 70 + 70 + 65)$$

$$= 900 + 270$$

$$= \text{Rs. } 1170$$

Step-2:

$$\text{Average Annual Return} = \frac{\text{Total Return}}{\text{No. of years}} = \frac{1170}{4}$$

In Rupee

$$= \text{Rs. } 292.5$$

Step-3:

$$\text{Average percentage Return} = \frac{292.5}{7000}$$

(Approximate Return)

$$= 4.17\%$$

Step-4:

Calculation of Net present Value (NPV)					
Year	Cash flow	PVIF@4%	PV	PVIF@3%	PV
1	65	0.9615	62.50	0.9709	63.11
2	70	0.9246	64.71	0.9426	65.98
3	70	0.8890	62.23	0.9151	64.06
4	65+7900=7965	0.8548	6808.52	0.8885	7076.80
			TPV = 6997.96	TPV = 7269.95	
			- CF ₀ = 7000	- CF ₀ = 7000	
			NPV = (2.04)	NPV = 269.95	

Step-5:

By Interpolation:

Low Rate (LR) = 3%

High Rate (HR) = 4%

NPV_{LR} = 269.95

NPV_{HR} = (2.04)

$$\begin{aligned}
 IRR &= LR + \frac{NPV_{LR}}{NPV_{LR} - NPV_{HR}} \times (HR - LR) \\
 &= 3\% + \frac{269.95}{269.95 + 2.04} \times (4\% - 3\%) \\
 &= 3.99\%
 \end{aligned}$$

Since, the Internal Rate of Return 3.99% is lower than the required rate of return of 5%, the Investment is not better.

Problem 4.12

Soln

Given:

Initial Investment (CF_0) = Rs. 25,000

Cash flow in Year 1 (CF_1) = 0

Cash flow in Year 2 (CF_2) = 0

Cash flow in Year 3 (CF_3) = Rs. 5000

Cash flow in Year 4 (CF_4) = Rs. 35,000

Step-1:

$$\begin{aligned}\text{Total Rupee Return} &= (35,000 - 25,000) + 5,000 \\ &= \text{Rs. } 15,000\end{aligned}$$

Step-2:

$$\begin{aligned}\text{Average rupee Return} &= \frac{15,000}{4} \\ &= \text{Rs. } 3,750\end{aligned}$$

Step-3:

$$\begin{aligned}\text{Approximate average percentage Return} &= \frac{3,750}{25,000} \\ &= 15\%\end{aligned}$$

Step-4:

Calculation of NPV

Year	Cash Flows	PVIF@15%	PV	PVIF@12%	PV
1	0	0.8696	0	0.8929	0
2	0	0.7561	0	0.7972	0

3	5000	0.6575	3287.5	0.7118	3558.9
4	35000	0.5718	20013	0.6355	22243.13
		TPV	23300.5	TPV	25802.03
		- CF ₀	25000	- CF ₀	25000
		NPV	(1699.5)	NPV	802.03

Step-5:

By Interpolation:

Low Rate (LR) = 12%

High Rate (HR) = 15%

NPV_{LR} = 802.03

NPV_{HR} = (1699.5)

$$IRR = LR + \frac{NPV_{LR}}{NPV_{LR} - NPV_{HR}} \times (HR - LR)$$

$$= 12\% + \frac{802.03}{802.03 + 1699.5} \times (15 - 12)$$

$$= 12.96\%$$

Since, the Internal Rate of Return is higher than the required rate of return, we would invest in the project.

Problem 4.13

Solⁿ

Stock 'X'

$$Div_{2015} = Div_{2009} (1+g)^6$$

$$5.25 = 4.21 (1+g)^6$$

$$\left(\frac{5.25}{4.21}\right)^{1/6} = 1+g$$

$$\therefore g = \left(\frac{5.25}{4.21}\right)^{1/6} - 1$$

$$= 3.75\%$$

Stock 'Y'

$$Div_{2015} = Div_{2011} (1+g)^4$$

$$3.20 = 2.69 (1+g)^4$$

$$\left(\frac{3.20}{2.69}\right)^{1/4} = 1+g$$

$$g = \left(\frac{3.20}{2.69}\right)^{1/4} - 1$$

$$= 4.43\%$$

Stock Y has higher annual compound rate of growth in dividend.

* Expected Rate of Return:

This is the return which is expected to be earned from the given investment in the future. It is largely affected by the change in economic conditions.

Data

Historical Data		Data with probability	
Year	Return	Probability	Return
1	10%	0.3	10%
2	5	0.4	5
3	15	0.1	15
4	-5	0.2	-5

Requirements:

1. Expected Rate of Return $E(R)$ / Average Return ($\bar{R}$)
2. Standard Deviation (σ)
3. Variance (σ^2)
4. Coefficient of Variation (CV)
5. Covariance between stock A and stock B (COV_{AB})
6. Correlation between stock A and stock B (ρ_{AB})
7. Portfolio
 - i. Portfolio Return
 - ii. Portfolio Risk

Problem 4.14

Solⁿ

Calculation of average return and standard deviation:

Year	R_H	R_B	$R_H - \bar{R}_H$	$R_B - \bar{R}_B$	$[R_H - \bar{R}_H]^2$	$[R_B - \bar{R}_B]^2$
1	10%	14%	-1	+12.87	1	7.13
2	15	-10	4	-21.93	16	454.96
3	8	30	-3	18.67	9	348.57
$\sum R_H = 33$ $\sum R_B = 34$			$\sum [R_H - \bar{R}_H]^2 = 26$		$\sum [R_B - \bar{R}_B]^2 = 810.64$	

a. Average Return of HBL stock ($\bar{R}_H$) = $\frac{\sum R_H}{n} = \frac{33}{3} = 11\%$

Average Return of BOK stock ($\bar{R}_B$) = $\frac{\sum R_B}{n} = \frac{34}{3} = 11.33\%$

b. Standard Deviation of HBL stock (σ_H) = $\sqrt{\frac{\sum [R_H - \bar{R}_H]^2}{n-1}}$
 $= \sqrt{\frac{26}{3-1}} = \sqrt{13} = 3.60\%$

Variance of HBL stock = $(\sigma_H)^2 = (3.60)^2 = 13$

Standard Deviation of BOK stock (σ_B) = $\sqrt{\frac{\sum [R_B - \bar{R}_B]^2}{n-1}}$
 $= \sqrt{\frac{810.64}{3-1}} = 20.13\%$

Variance of BOK stock = $(\sigma_B)^2 = (20.13)^2 = 405.34$

Stock BOK has higher variance and standard deviation

c. Calculation of Coefficient of Variation (CV)

$$CV_H = \frac{\sigma_H}{\bar{R}_H} = \frac{3.60}{11} = 0.32$$

$$CV_B = \frac{\sigma_B}{\bar{R}_B} = \frac{20.13}{11.33} = 1.77$$

Stock BOK is more riskier due to higher cv.

Problem 4.15

Solⁿ

a. On the basis of a review of the return data, stock A appears to be more risky due to higher fluctuation in return.

b. Calculation of Average Return and standard Deviation:

Year	R_A	R_B	$R_A - \bar{R}_A$	$R_B - \bar{R}_B$	$[R_A - \bar{R}_A]^2$	$[R_B - \bar{R}_B]^2$
2011	19%	8%	7%	-4	49	16
2012	1	10	-11	-2	121	4
2013	10	12	-2	0	4	0
2014	26	14	14	2	196	4
2015	4	16	-8	4	64	16
$\Sigma R_A = 60$ $\Sigma R_B = 60$					$\Sigma [R_A - \bar{R}_A]^2 = 434$	$\Sigma [R_B - \bar{R}_B]^2 = 40$

$$\text{Average Return of Investment A } [\bar{R}_A] = \frac{\sum R_A}{n} = \frac{60}{5} = 12\%$$

$$\text{Average Return of Investment B } [\bar{R}_B] = \frac{\sum R_B}{n} = \frac{60}{5} = 12\%$$

c. Calculation of Standard Deviation:

Standard Deviation of Investment A

$$\sigma_A = \sqrt{\frac{\sum [R_A - \bar{R}_A]^2}{n-1}} = \sqrt{\frac{434}{5-1}} = 10.42\%$$

Standard Deviation of Investment B

$$\sigma_B = \sqrt{\frac{\sum [R_B - \bar{R}_B]^2}{n-1}} = \sqrt{\frac{40}{5-1}} = 3.16\%$$

d. On the basis of our calculation in part 'c', Investment A is more risky due to higher standard deviation. The result in part 'a' is same as in part 'c' because higher fluctuation in returns results higher risk.

Problem 4.16

Solⁿ

a. Calculation of expected Return and standard deviation

state of economy	Prob. (P)	R	$P \times R$	$R - E(R)$	$P[R - E(R)]^2$
Strong growth	0.10	25%	2.5	13.7	18.769
Moderate growth	0.40	15	6	3.7	5.476
Weak growth	0.40	10	4	-1.3	0.676
Recession	0.10	-12	-1.2	-23.3	54.289
			$\sum P_j \times R$		$\sum P_j [R - E(R)]^2$
			= 11.3		= 79.21

∴ Expected Rate of Return, $E(R) = \sum P_j \times R = 11.3\%$

b. Variance = $\sum P_j [R - E(R)]^2 = 79.21$

c. Standard Deviation (σ) = $\sqrt{\sum P_j [R - E(R)]^2} = \sqrt{79.21} = 8.9\%$

d. Coefficient of Variation (CV) = $\frac{\sigma}{E(R)} = \frac{8.9}{11.3} = 0.7876$

e. The coefficient of variation is a relative measure of risk. It relates investment risk to the return. It measures risk per unit of return.

Problem 4.17

solⁿ

Calculation of expected Return and standard deviation:

Prob.(P)	R _x	R _y	P _j × R _x	P _j × R _y	R _x - E(R _x)	R _y - E(R _y)	P _j [R _x - E(R _x)] ²
0.2	5%	50%	1	10	-7.5	30	11.25
0.3	10	30	3	9	-2.5	10	1.875
0.3	15	10	4.5	3	2.5	-10	1.875
0.2	20	-10	4	-2	7.5	-30	11.25
			Σ P _j × R _x	Σ P _j × R _y			
			= 12.5%	= 20%			
						Σ P _j [R _x - E(R _x)] ²	= 26.25

a. Expected Return of stock X, $E(R_x) = \sum P_j \times R_x$	$P_j [R_y - E(R_y)]^2$
= 12.5%	180
Expected Return of stock Y, $E(R_y) = \sum P_j \times R_y$	30
= 20%	30
	180
	$\Sigma P_j [R_y - E(R_y)]^2 = 420$

b. Standard Deviation of stock X

$$\sigma_x = \sqrt{\sum P_j [R_x - E(R_x)]^2} = \sqrt{26.25} = 5.12\%$$

Standard Deviation of stock Y

$$\sigma_y = \sqrt{\sum P_j [R_y - E(R_y)]^2} = \sqrt{420} = 20.49$$

c. Calculation of coefficient of variation (cv)

$$CV_X = \frac{\sigma_X}{E(R_X)} = \frac{5.12}{12.5} = 0.4096$$

$$CV_Y = \frac{\sigma_Y}{E(R_Y)} = \frac{20.49}{20} = 1.0245$$

Stock Y is more riskier due to higher cv. so, we should prefer stock X with lower cv.

Problem 4.18

Solⁿ

q. Calculation of Expected Return and standard deviation of stock X

Prob. (P _j)	R _X	P _j × R _X	R _X - E(R _X)	P _j [R _X - E(R _X)] ²
0.1	-10%	-1	-22%	48.4
0.2	2	0.4	-10%	20
0.4	12	4.8	0	0
0.2	20	4	8	12.8
0.1	38	3.8	26	67.6
$\Sigma P_j \times R_X = 12$			$\Sigma P_j [R_X - E(R_X)]^2 = 148.8$	

∴ The expected return of stock X, $E(R_X) = \Sigma P_j \times R_X = 12\%$

∴ Standard deviation of stock X, $\sigma_X = \sqrt{\Sigma P_j [R_X - E(R_X)]^2}$
 $= \sqrt{148.8} = 12.20\%$

b. Calculation of Expected Return and standard deviation of stock Y.

Prob (P _i)	R _Y	P _j × R _Y	R _Y - E(R _Y)	P _j (R _Y - E(R _Y)) ²
0.1	-35%	-3.5	-49%	240.1
0.2	0	0	-14	39.2
0.4	20	8	6	14.4
0.2	25	5	11	24.2
0.1	45	4.5	31	96.1
$\sum P_j \times R_j = 14\%$			$\sum P_j [R_Y - E(R_Y)]^2 = 414$	

∴ The expected return of stock Y, $E(R_Y) = \sum P_j \times R_j = 14\%$

∴ Standard deviation of stock Y, $\sigma_Y = \sqrt{\sum P_j [R_Y - E(R_Y)]^2}$
 $= \sqrt{414} = 20.35\%$

c. Coefficient of variation, $CV_X = \frac{\sigma_X}{E(R_X)} = \frac{12.20}{12} = 1.02$

Coefficient of variation, $CV_Y = \frac{\sigma_Y}{E(R_Y)} = \frac{20.35}{14} = 1.45$

d. NO, it is not possible that most of the investors might regard stock Y as being less risky than stock X because stock Y has higher standard deviation and coefficient of variation than stock X.

Problem 4.19

Soln

a. Calculation of Holding Period Return and expected Return (stock A)

Year	D_1	P_0	P_1	HPR = $\frac{P_1 - P_0 + D_1}{P_0} \times 100$
2011	1.6	23	26	20%
2012	1.7	26	25	2.69%
2013	2.0	25	24	4%
2014	2.1	24	27	21.25%
2015	2.2	27	30	19.26%
				$\Sigma \text{HPR} = 67.2\%$

$$\% \text{ Expected Return, } E(R_A) = \frac{\Sigma \text{HPR}_A}{n} = \frac{67.2}{5} = 13.44\%$$

For stock B:

Year	D_1	P_0	P_1	HPR = $\frac{P_1 - P_0 + D_1}{P_0} \times 100$
2011	2.0	22	23	13.64%
2012	2.1	23	23	9.13
2013	2.2	23	24	13.91
2014	2.3	24	25	13.75
2015	2.4	25	25	9.6
				$\Sigma \text{HPR} = 60.03\%$

$$\% \text{ Expected Return, } E(R_B) = \frac{\Sigma \text{HPR}_B}{n} = \frac{60.03\%}{5} = 12.01\%$$

b. Calculation of standard deviation and CV (Stock X)

Year	R_X	$R_X - E(R_X)$	$[R_X - E(R_X)]^2$
2011	20%	6.56%	42.03
2012	2.69	-10.75	115.56
2013	4	-9.44	89.11
2014	21.25	7.81	61
2015	19.26	5.82	33.87
			$\Sigma [R_X - E(R_X)]^2 = 342.57$

$$\therefore \text{Standard deviation } (\sigma_A) = \sqrt{\frac{\Sigma [R_A - E(R_A)]^2}{n-1}} = \sqrt{\frac{342.57}{5-1}} = 9.25\%$$

$$\therefore \text{Coefficient of Variation } (CV_A) = \frac{\sigma_A}{E(R_A)} = \frac{9.25}{13.44} = 0.69$$

Stock 'B'

Year	R_B	$R_B - E(R_B)$	$[R_B - E(R_B)]^2$
2011	13.64	1.63	2.65
2012	9.13	-2.88	8.29
2013	13.91	1.9	3.61
2014	13.75	1.74	3.03
2015	9.6	-2.41	5.81
			$\Sigma [R_B - E(R_B)]^2 = 23.39$

$$\therefore \text{Standard Deviation } (\sigma_B) = \sqrt{\frac{\Sigma [R_B - E(R_B)]^2}{n-1}} = \sqrt{\frac{23.39}{5-1}} = 2.41\%$$

$$\therefore \text{Coefficient of Variation } (CV_B) = \frac{\sigma_B}{E(R_B)} = \frac{2.41}{12.01} = 0.20$$

c. The expected return of stock A is greater than that of stock B where its standard deviation of stock B is less than stock A. Considering rate of return stock A is preferable due to higher return but stock B is also preferable due to lower standard deviation. So there is a conflict between return and risk.

Finally we should use the relative measure i.e. coefficient of variation to make the conclusion. Therefore, stock B is preferable due to lower CV.

d. We would recommend Nilima to invest in stock B due to lower coefficient of variation.

