

T.U. - 2076

Rita established a scholarship scheme that promises to pay needy students Rs 180,000 per year forever. How much should she deposit today to get this perpetual payment if the required interest rate is 12%?

Given,

PMT = Rs. 180,000

Interest rate (i) = 12%

P.Va (perpetual payment) = PMT / i

$$180,000 / 0.12$$

$$= \text{Rs. } 15,00,000$$

Per year, Each year, Every year, Equal installment = PMT

Current, Now, past year, deposited, last year = PV

Accumulated, Will, Will be, future, expected = FV

$$F.V = P.V(1+i)^n$$

$$P.V = \frac{F.V}{(1+i)^n}$$

T.U. - 2073

Nepal Bank Ltd pays 6 percent interest on its saving deposit. What is the effective interest rate if it is compounded quarterly?

Given,

Quarterly (m) = 3, 3, 3, 3 = 4

Semi-annually (m) = 6, 6 = 2

Interest Rate = i/m

No. of year = n*m

Effective annual Interest rate = $(1 + i/m)^m - 1$

$$= (1 + 0.06/4)^4 - 1$$

$$= 6.14\%$$

Descriptive Answer Questions

T.U. - 2076

Mr. Rajesh Devkota needs to accumulate Rs 1,000,000 to buy a second-hand vehicle for his personal use. He can save only Rs 125,000 annually out of his earnings, which can be deposited in a bank account at 12 percent annual compound interest rate. His last deposit will be less than Rs 125,000 if less is needed to round out to Rs 1,000,000. How many years will it take Mr. Devkota to reach his Rs 1,000,000 goal? How large will the last deposit be? (6+4)

Given,

FV_A = Rs. 10,00,000

Pmt = Rs. 125,000

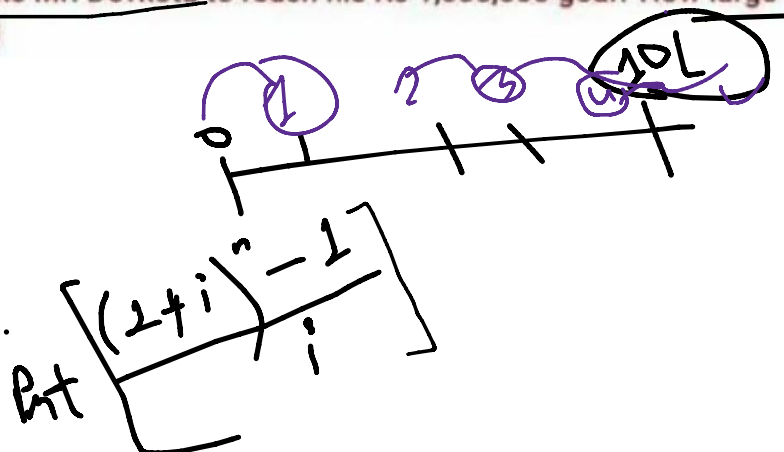
Interest (i) = 12%

No. of year (n) = ?

Now,

$$F.V_A = Pmt \times FVIFA_{i\%, n \text{ year}}$$

$$F.V_A = 125000 \frac{(1+i)^n - 1}{i}$$



$$\frac{10,00,000}{125,000} = \frac{(1+0.12)^n - 1}{0.12}$$

$$\text{Or, } 8 \times 0.12 = (1.12)^n - 1$$

$$\text{Or, } 0.96 + 1 = (1.12)^n$$

$$\text{Or, } 1.96 = (1.12)^n$$

Or, Taking log on both side

$$\text{Or, } \log 1.96 = n \log 1.12$$

$$\text{Or, } \frac{\log 1.96}{\log 1.12} = n$$

$$\text{Or, } N = 5.93 \text{ year or 6 year}$$

The number of year is 6 year

For his last deposit of less than 125000

We need a calculation for the 5 years

$$F.V.A = \text{Pmt} \times \text{FVIFA } i\%, n \text{ year } (i+1)$$

$$= 125000 \times \text{FVIFA } 12\%, 5 \text{ year } (0.12+1)$$

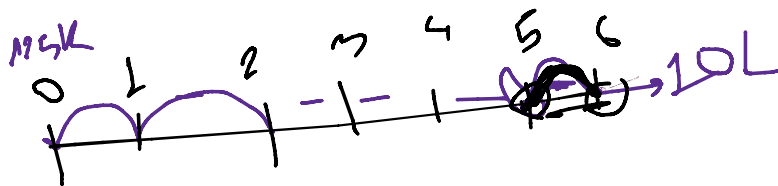
$$= 125000 \times 6.3528 (1.12)$$

$$= 8,89,392$$

Last deposit

$$10,00,000 - 8,89,392$$

$$= \text{Rs. } 1,10,608$$



FUTURE VALUE INTEREST FACTOR (FVIFA) OF AN ANNUITY THAT STARTS IN 1 PERIOD AND LASTS T PERIODS (ORDINARY ANNUITY)

| Time (T) | Interest Rate (R) | | | | | | | | | | | | | | | | | | | |
|----------|-------------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|---------|----------|----------|----------|----------|----------|----------|----------|----------|----------|
| | 1% | 2% | 3% | 4% | 5% | 6% | 7% | 8% | 9% | 10% | 11% | 12% | 13% | 14% | 15% | 16% | 17% | 18% | 19% | 20% |
| 1 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 | 1.0000 |
| 2 | 2.0100 | 2.0200 | 2.0300 | 2.0400 | 2.0500 | 2.0600 | 2.0700 | 2.0800 | 2.0900 | 2.1000 | 2.1100 | 2.1200 | 2.1300 | 2.1400 | 2.1500 | 2.1600 | 2.1700 | 2.1800 | 2.1900 | 2.2000 |
| 3 | 3.0301 | 3.0604 | 3.0909 | 3.1216 | 3.1525 | 3.1836 | 3.2149 | 3.2464 | 3.2781 | 3.3100 | 3.3421 | 3.3744 | 3.4069 | 3.4396 | 3.4725 | 3.5056 | 3.5389 | 3.5724 | 3.6061 | 3.6400 |
| 4 | 4.0604 | 4.1216 | 4.1836 | 4.2465 | 4.3101 | 4.3746 | 4.4399 | 4.5061 | 4.5731 | 4.6410 | 4.7097 | 4.7793 | 4.8498 | 4.9211 | 4.9934 | 5.0665 | 5.1405 | 5.2154 | 5.2913 | 5.3680 |
| 5 | 5.1010 | 5.2040 | 5.3091 | 5.4163 | 5.5256 | 5.6371 | 5.7507 | 5.8666 | 5.9847 | 6.1051 | 6.2278 | 6.3528 | 6.4803 | 6.6101 | 6.7424 | 6.8771 | 7.0144 | 7.1542 | 7.2966 | 7.4416 |
| 6 | 6.1520 | 6.3081 | 6.4684 | 6.6330 | 6.8019 | 6.9753 | 7.1533 | 7.3359 | 7.5233 | 7.7156 | 7.9129 | 8.1152 | 8.3227 | 8.5355 | 8.7537 | 8.9775 | 9.2068 | 9.4420 | 9.6830 | 9.9299 |
| 7 | 7.2135 | 7.4343 | 7.6625 | 7.8983 | 8.1420 | 8.3938 | 8.6540 | 8.9228 | 9.2004 | 9.4872 | 9.7833 | 10.0890 | 10.4047 | 10.7305 | 11.0668 | 11.4139 | 11.7720 | 12.1415 | 12.5227 | 12.9159 |
| 8 | 8.2857 | 8.5830 | 8.8923 | 9.2142 | 9.5491 | 9.8975 | 10.2598 | 10.6366 | 11.0285 | 11.4359 | 11.8594 | 12.2997 | 12.7573 | 13.2328 | 13.7268 | 14.2401 | 14.7733 | 15.3270 | 15.9020 | 16.4991 |
| 9 | 9.3685 | 9.7546 | 10.1591 | 10.5828 | 11.0266 | 11.4913 | 11.9780 | 12.4876 | 13.0210 | 13.5795 | 14.1640 | 14.7757 | 15.4157 | 16.0853 | 16.7858 | 17.5185 | 18.2847 | 19.0859 | 19.9234 | 20.7989 |
| 10 | 10.4622 | 10.9497 | 11.4639 | 12.0061 | 12.5779 | 13.1808 | 13.8164 | 14.4866 | 15.1929 | 15.9374 | 16.7220 | 17.5487 | 18.4197 | 19.3373 | 20.3037 | 21.3215 | 22.3931 | 23.5213 | 24.7089 | 25.9587 |
| 11 | 11.5668 | 12.1687 | 12.8078 | 13.4864 | 14.2068 | 14.9716 | 15.7836 | 16.6455 | 17.5603 | 18.5312 | 19.5614 | 20.6546 | 21.8143 | 23.0445 | 24.3493 | 25.7329 | 27.1999 | 28.7551 | 30.4035 | 32.1504 |
| 12 | 12.6825 | 13.4121 | 14.1920 | 15.0258 | 15.9171 | 16.8699 | 17.8885 | 18.9771 | 20.1407 | 21.3843 | 22.7132 | 24.1331 | 25.6502 | 27.2707 | 29.0017 | 30.8502 | 32.8239 | 34.9311 | 37.1802 | 39.5805 |
| 13 | 13.8093 | 14.6803 | 15.6178 | 16.6268 | 17.7130 | 18.8821 | 20.1406 | 21.4953 | 22.9534 | 24.5227 | 26.2116 | 28.0291 | 29.9847 | 32.0887 | 34.3519 | 36.7862 | 39.4040 | 42.2187 | 45.2445 | 48.4966 |
| 14 | 14.9474 | 15.9739 | 17.0863 | 18.2919 | 19.5986 | 21.0151 | 22.5505 | 24.2149 | 26.0192 | 27.9750 | 30.0949 | 32.3926 | 34.8827 | 37.5811 | 40.5047 | 43.6720 | 47.1027 | 50.8180 | 54.8409 | 59.1959 |
| 15 | 16.0969 | 17.2934 | 18.5989 | 20.0236 | 21.5786 | 23.2760 | 25.1290 | 27.1521 | 29.3609 | 31.7725 | 34.4054 | 37.2797 | 40.4175 | 43.8424 | 47.5804 | 51.6595 | 56.1101 | 60.9653 | 66.2607 | 72.0351 |
| 16 | 17.2579 | 18.6393 | 20.1569 | 21.8245 | 23.6575 | 25.6725 | 27.8881 | 30.3243 | 33.0034 | 35.9497 | 39.1899 | 42.7533 | 46.6717 | 50.9804 | 55.7175 | 60.9250 | 66.6488 | 72.9390 | 79.8502 | 87.4421 |
| 17 | 18.4304 | 20.0121 | 21.7616 | 23.6975 | 25.8404 | 28.2129 | 30.8402 | 33.7502 | 36.9737 | 40.5447 | 44.5008 | 48.8837 | 53.7391 | 59.1176 | 65.0751 | 71.6730 | 78.9792 | 87.0680 | 96.0218 | 105.9306 |
| 18 | 19.6147 | 21.4123 | 23.4144 | 25.6454 | 28.1324 | 30.9057 | 33.9990 | 37.4502 | 41.3013 | 45.5992 | 50.3959 | 55.7497 | 61.7251 | 68.3941 | 75.8364 | 84.1407 | 93.4056 | 103.7403 | 115.2659 | 128.1167 |
| 19 | 20.8109 | 22.8406 | 25.1169 | 27.6712 | 30.5390 | 33.7600 | 37.3790 | 41.4463 | 46.0185 | 51.1591 | 56.9395 | 63.4397 | 70.7494 | 78.9692 | 88.2118 | 98.6032 | 110.2846 | 123.4135 | 138.1664 | 154.7400 |
| 20 | 22.0190 | 24.2974 | 26.8704 | 29.7781 | 33.0660 | 36.7856 | 40.9955 | 45.7620 | 51.1601 | 57.2750 | 64.2028 | 72.0524 | 80.9468 | 91.0249 | 102.4436 | 115.3797 | 130.0329 | 146.6280 | 165.4180 | 186.6880 |
| 21 | 23.2392 | 25.7833 | 28.6765 | 31.9692 | 35.7193 | 39.9927 | 44.8652 | 50.4229 | 56.7645 | 64.0025 | 72.2651 | 81.6987 | 92.4699 | 104.7684 | 118.8101 | 134.8405 | 153.1385 | 174.0210 | 197.8474 | 225.0256 |
| 22 | 24.4716 | 27.2990 | 30.5368 | 34.2480 | 38.5052 | 43.3923 | 49.0057 | 55.4568 | 62.8733 | 71.4027 | 81.2143 | 92.5026 | 105.4910 | 120.4360 | 137.6316 | 157.4150 | 180.1721 | 206.3448 | 236.4385 | 271.0307 |
| 23 | 25.7163 | 28.8450 | 32.4570 | 36.6170 | 41.4305 | 46.9058 | 53.4361 | 60.8933 | 69.3310 | 79.6430 | 91.1470 | 104.0209 | 118.7048 | 134.7070 | 152.7764 | 183.6014 | 211.8013 | 244.8868 | 283.3817 | 326.7469 |

T.U. - 2075

You need to accumulate Rs 100,000. To do so, you plan to make deposits of Rs 17,500 per year, with the first payment being made a year from today, in a bank account which pays 6 percent annual interest. Your last deposit will be more than Rs 17,500 if more is needed to round out to Rs 100,000. How many years will it take you to reach your goal of Rs 100,000, and how large will the last deposit be? (6+4)

Pmt

Solution,

Given

$$F.V = \text{Rs. } 100,000$$

T.U. - 2074

The management of Vikash publication decided to buy a printing press by taking a loan of Rs 1,000,000 for 3 years from Nepal Bank Limited. The loan bears a compound annual interest rate of 10 percent and calls for equal annual installment payments at the end of each year for 3 years.

- What is the amount of annual payments?
- Prepare loan amortization schedule.
- What fraction of payment made in year 2 represents the principal? (4+4+2)

Given,

PVA = Rs. 10,00,000 (Loan)

Number of years (n) = 3 years

Interest rate (i) = 10%

$PVA = \text{Pmt} \times PVIFA_{i\%, n\text{year}}$

$10,00,000 = \text{pmt} \times PVIFA_{10\%, 3\text{ years}}$

$\text{Pmt} = \frac{10,00,000}{2.4869}$

Pmt = Rs. 4,02,107

Annual payment Rs. 3,02,115

Calculation of loan amortization schedule:

| Year | Beginning loan | Payment(pmt) 3 | Interest(10%) 4 | Principal (3-4=5) | Ending loan 2-5=6 |
|------|----------------|-------------------|--------------------|----------------------|----------------------|
| 1 | 10,00,000 | 4,02,107 | 1,00,000 | 3,02,107 | 6,97,893 |
| 2 | 6,97,893 | 4,02,107 | 69789.3 | 332377.5 | 3,65,575.3 |
| 3 | 3,65,575.3 | 4,02,107 | 36557.53 | 365549.47 | 25.83 |

25.83 is a calculation of rounding error. They will manage it during the settlement process.

- Fraction of payment represents to the principle for 2 year

Principle

Payment

$$\frac{332377.5}{402,107}$$

82.65%

T.U. - 2073

The management of Delta Trading Company decided to buy a delivery van taking a loan of Rs 1,200,000 for 4 years from Nepal Bank. The loan bears an annual interest of 10 percent and calls for equal annual installment payments at the end of each of the 4 years.

- Determine amount of annual payment.
- Prepare loan amortization schedule. (4+6)

Sakyo sabbai?

H.W

Assume that it is now January 1, 2013. On January 1, 2014, you will deposit Rs 1,000 into a savings account that pays 8 percent.

(a) If the bank compounded interest annually, how much will you have in your account on January 1, 2017?

(b) What would your January 1, 2017 balance be if the bank used quarterly compounding rather than annual compounding?

(c) Suppose you deposit the Rs 1,000 in 4 payments of Rs 250 each on January 1 of 2014, 2015, 2016 and 2017. How much would you have in your account on January 1, 2017, based on 8 percent annual compounding?

(c) Suppose you deposit 4 equal installments in your account on January 1 of 2014, 2015, 2016, and 2017. Assuming an 8 percent interest rate, how large would each of your payments have to be for you to obtain the same ending balance as you calculated in part (a)? (2.5×4)

Given,

P.V = Rs. 1000 Interest rate (i) = 8% Number of year (n) = 3 year

a) $F.V = P.V (1+i)^n$

$$= 1000(1+0.08)^3$$

$$= \text{Rs. } 1259.712$$

b) $F.V = P.V(1+i/4)^{n*4}$

$$1000(1+0.08/4)^{4*3}$$

$$= \text{Rs. } 1268.24$$

c) $Pmt = \text{Rs. } 250$

$$FVA = Pmt * FVIFA_{i\%, n \text{ year}}$$

$$= 250 * FVIFA_{8\%, 4 \text{ year}}$$

$$= 250 * 4.5061$$

$$= \text{Rs. } 1126.525$$

d) Given, $PMT = ?$

$$FVA = \text{Rs. } 1259.712 \quad \text{interest rate (i) = 8\%}$$

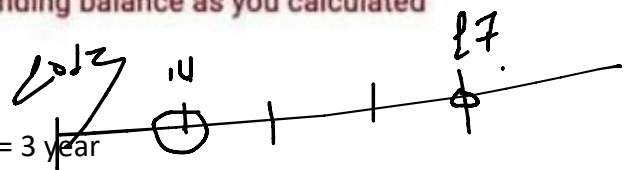
$$FVA = Pmt * FVIFA_{i\%, n \text{ year}}$$

$$1259.712 = pmt * FVIFA_{8\%, 4 \text{ year}}$$

$$\text{Or, } 1259.712 = Pmt$$

$$\frac{4.5061}{}$$

$$: Pmt = \text{Rs. } 279.55$$



Answer the following:

(a) What is the future value of 5-year annuity due that promises to pay out Rs. 400 each year? Assume all payments are reinvested at 7% a year, until year 5.

(b) You decided to buy a car, and a local bank is willing to lend you Rs 500,000 to buy a Nano car. Under the terms of the loan, it will be fully amortized over 60 months, and the nominal rate of interest will be 12 percent, with interest paid monthly. What would be the monthly payment on the loan? What is the effective rate of interest?

(c) Your client is 40 years old and wants to begin saving for retirement. You advise the client to put Rs. 6,000 a year into the stock market. You estimate that the markets return will be, on average, 12 percent a year. Assume the investment will be made the end of the year. How much will he/she have by age 70?

Given,

FVA = ? Number of year = 5 year Pmt = Rs.400 Interest rate(i) = 7%

Due = ? (1+i)

$$\begin{aligned} \text{FVA} &= \text{PMT} \times \text{FVIFA}_{i\%, n\text{year}} (1+i) \\ &= 400 \times \text{FVIFA}_{7\%, 5\text{year}} (1+0.07) \\ &= \text{Rs. } 2461.3 \end{aligned}$$

Given,

Loan (PVA) = Rs.500000

Number of year(n) = 60month = 5 year

Interest rate (i) = 12% or 12%/12 = 1%

PVA = Pmt * PVIFA_{i%, Nyear}

$$500000 = \text{Pmt} \times \text{PVIFA}_{1\%, 60\text{month}}$$

$$500000 = \text{pmt} \times$$

$$\left[\frac{1 - \frac{1}{(1+i)^n}}{i} \right]$$

$$\text{Pmt} = \text{Rs. } 11,222.23$$

$$\begin{aligned} \text{Effective annua rate} &= [1 + (i/m)]^n - 1 \\ &= [1 + (0.12/12)]^{12} - 1 \\ &= \text{Rs. } 12.68\% \end{aligned}$$

Risk and Return Finance- 15 + 2= 17 Marks

Fixed

Formula: Session

There are mainly two types of Exam

Historical Data (Year is given)

Probability Data (% probability or decimal probability given)

Requirements:

Expected / Average return ($\sum R_A$) = $\sum R_A / n$ (If There is no probability)
= $\sum R_A * P$ (If there is probability)

Requirements:

1. Average / Expected Return ($\bar{R} / E(R)$)

2. Standard Deviation (σ)

3. Variance (σ^2)

4. Coefficient of Variation (cv)

5. Covariance between stock A and stock B (C)

6. Correlation between stock A and stock B

7. Portfolio: i. Portfolio Return (R_p)

ii. Portfolio Risk (σ_p)

8. Required Rate of Return

9. Security Market Line (SML)

10. Beta (β)

1. Average Return (\bar{R})

$$\bar{R}_A = \frac{\sum R_A}{n}$$

$$\bar{R}_B = \frac{\sum R_B}{n}$$

2. Standard Deviation (σ)

$$\sigma_A = \sqrt{\frac{\sum [R_A - \bar{R}_A]^2}{n-1}}$$

$$\sigma_B = \sqrt{\frac{\sum [R_B - \bar{R}_B]^2}{n-1}}$$

$$COV_{AB} = \frac{[R_A - \bar{R}_A][R_B - \bar{R}_B]}{n-1}$$

1. Rate of Return (R) = $\frac{P_1 - P_0 + D_1}{P_0}$

current yield = $\frac{D_1}{P_0}$ and capital gain yield = $\frac{P_1 - P_0}{P_0}$

Rate of Return = current yield + capital gain yield.

where,

P_1 = Ending price of investment or selling price

P_0 = beginning price of investment or purchase price

D_1 = year end income i.e. interest or dividend income

2. Expected Return or Average Return (\bar{R}_A) = $\sum R_A \cdot P_r$ OR $\frac{\sum R_A}{N}$

3. standard deviation of stock A (σ_A) = $\sqrt{\frac{\sum (R_A - \bar{R}_A)^2}{N-1}}$ OR $\sqrt{\frac{\sum (R_A - \bar{R}_A)^2}{N-1}}$

4. Coefficient of variation of stock A (CVA) = $\frac{\sigma_A}{\bar{R}_A}$

5. Expected Return or Average Return on portfolio (\bar{R}_{AB}):

$\sum R_{AB} \cdot P_r$ OR $\sum R_{AB}$ OR $W_A \cdot \bar{R}_A + W_B \cdot \bar{R}_B$ and

$R_{AB} = W_A \cdot R_A + W_B \cdot R_B$

σ_P

SP

σ_P

$$\sigma_{AB} = \sqrt{w_A^2 \cdot \sigma_A^2 + w_B^2 \cdot \sigma_B^2 + 2 \cdot w_A \cdot w_B \cdot \rho_{AB} \cdot \sigma_A \cdot \sigma_B}$$
$$\sigma_{ABC} = \sqrt{w_A^2 \cdot \sigma_A^2 + w_B^2 \cdot \sigma_B^2 + w_C^2 \cdot \sigma_C^2 + 2 \cdot w_A \cdot w_B \cdot \rho_{AB} \cdot \sigma_A \cdot \sigma_B + 2 \cdot w_B \cdot w_C \cdot \rho_{BC} \cdot \sigma_B \cdot \sigma_C + 2 \cdot w_A \cdot w_C \cdot \rho_{AC} \cdot \sigma_A \cdot \sigma_C}$$

1. coefficient of variation (CV_{AB}) = $\frac{\sigma_{AB}}{\bar{R}_{AB}}$

2. co-variance between return on stock A and stock B (COV_{AB})

$$COV_{AB} = \frac{\sum (R_A - \bar{R}_A)(R_B - \bar{R}_B) \times pr}{N-1} \text{ OR } \frac{\sum (R_A - \bar{R}_A)(R_B - \bar{R}_B)}{N-1} \text{ OR } \rho_{AB} \cdot \sigma_A \cdot \sigma_B$$

3. Correlation between Return on stock A and stock B

$$\rho_{AB} = \frac{COV_{AB}}{\sigma_A \cdot \sigma_B}$$

10. capital Assets pricing model (CAPM)

$$\text{Required Rate of Return (RA)} = \left[R_f + (R_m - R_f) \times \beta_A \right]$$

Market return premium ($R_m - R_f$)

11. Beta coefficient of stock A (β_A) = $\frac{COV_{AM}}{\sigma_M^2}$

12. Beta portfolio = $w_A \cdot \beta_A + w_B \cdot \beta_B + w_C \cdot \beta_C + \dots + w_n \cdot \beta_n$

13. slope of SML = $\frac{R_m - R_f}{\beta_m}$

Unit 4: Fundamentals of Risk and Return

Theoretical Questions

Brief Answer Questions

1. 2080 Q.No. 3

What is beta coefficient and what objective does it serve?

2. 2078 Q.No. 3

Define the term risk. How is it measured?

3. 2077 Q.No. 3

Define the term portfolio.

Descriptive Answer Questions

4. 2074 Q.No. 10a

Write notes on portfolio opportunity set.

5. 2072 Q.No. 10b

Write short note on efficient sets.

6. 2057

Explain the concept of portfolio risk and the capital assets pricing model.

Numerical Problems

1. 2079 Q.No. 9

Stock Y has a beta of 1.45 and expected return of 17 percent. If the risk free rate is 6 percent and market risk premium is 7.5 percent. Is the stock correctly priced?

2. 2077 Q.No. 7 2073 Q. No. 7

Assume that the risk-free rate is 6 percent and the market risk premium is 8 percent. Beta of Stock J is 1.5. Calculate required rate of return on Stock J.

3. 2076 Q.No. 4

Suppose you invested Rs 35,000 in Stock A that has a beta coefficient of 0.8 and Rs 40,000 in stock B that has a beta coefficient of 1.4. What is your portfolio's beta?

4. 2075 Q.No. 7

Assume that the risk-free rate is 8 percent and the market risk premium is 6 percent. Beta of Stock J is 2. Average rate of return on Stock J is 18 percent. Is Stock J correctly priced?

5. 2074 Q.No. 4

A portfolio consists of Stock A and Stock B with beta 0.9 and 1.6, respectively. If Stock A consists of 80 percent investment in the portfolio, what will be the portfolio beta?

$$\beta_A = \frac{\text{COV}_{Am}}{\sigma_m^2}$$

$\sigma, \text{C.V.}$

Given, Beta of stock Y = 1.45

Expected return = 17%

Rate = 6%

Market risk premium (R_m-R_f) = 7.5%

3) Stock A = 35000, Stock B = 40000

Total stock = 75,000

Weight of stock A (W_a) = 35,000 / 75,000 = 0.47

Weight of stock B (W_b) = 40,000 / 75,000 = 0.53

Beta coeff. Stock A = 0.8

Portfolio beta = W_a*B_a + W_b*B_b

= 0.47*0.8 + 0.53*1.4

= 1.118

B_p =

6. 2077 Q.No. 7 2073 Q. No. 7

Assume that the risk-free rate is 6 percent and the market risk premium is 8 percent. Beta of Stock J is 1.5. Calculate required rate of return on Stock J.

Ans: 18%

7. 2076 Q.No. 4

Suppose you invested Rs 35,000 in Stock A that has a beta coefficient of 0.8 and Rs 40,000 in stock B that has a beta coefficient of 1.4. What is your portfolio's beta?

Ans: 1.12

8. 2075 Q.No. 7

Assume that the risk-free rate is 8 percent and the market risk premium is 6 percent. Beta of Stock J is 2. Average rate of return on Stock J is 18 percent. Is Stock J correctly priced?

Ans: E(R_j) 20%

9. 2074 Q.No. 4

A portfolio consists of Stock A and Stock B with beta 0.9 and 1.6, respectively. If Stock A consists of 80 percent investment in the portfolio, what will be the portfolio beta?

Ans: 1.04

Risk-free rate (R_f) = 6%

Market risk premium ($R_f - R_m$) = 8%

Beta stock j (β) = 1.5

Rate of return = $R_f + (R_f - R_m) * \beta$
= $6\% + (8\% * 1.5)$
= 18%

7. 2076 Q.No. 4

Suppose you invested Rs 35,000 in Stock A that has a beta coefficient of 0.8 and Rs 40,000 in stock B that has a beta coefficient of 1.4. What is your portfolio's beta? [2]

Ans: 1.12

Given .

Stock A = Rs.35,000

Stock B = Rs. 40,000

Total Stock = 75,000

Weight of stock A (W_a) = $\frac{35,000}{75,000}$
= 46.67

Weight of stock B (W_b) = $\frac{40,000}{75,000}$
= 53.33

Beta coefficient of stock (A) = 0.8

2074 Q.No. 4

Consider the following information:

| State of Economy | Probability | Rate of return | |
|------------------|-------------|----------------|---------|
| | | Stock A | Stock B |
| Recession | 0.20 | 6% | (20%) |
| Normal | 0.60 | 7 | 13 |
| Boom | 0.20 | 11 | 33 |

Calculate: (a) Expected return of both stocks, (b) Standard deviation of both stocks, and (c) Covariance between return of both stocks. [3+3+4]

Ans: (a) 7.6% and 10.4% (b) 1.74% and 17.06 (c) 24.16

2077 Q.No. 12

Consider the following information associated with Stock A and Stock B given in the following table.

| | Stock A | Stock B |
|---------------------------------------------|---------|---------|
| Average rate of return | 12% | 18% |
| Standard deviation of returns | 6% | 8% |
| Covariance of stock returns | -38.4 | |
| Coefficient of correlation of stock returns | -0.8 | |

- Which one stock is more risky? Which one stock would you prefer? [2]
- If you form a portfolio of Stock A and Stock B comprising 60 percent wealth in Stock A and the rest in Stock B, calculate the risk and return of your portfolio. [4]
- Assume risk-free rate and market return are 8% and 15% respectively. Covariance between Stock A and market return is 54 and variance of market return is 36, calculate beta of Stock A. what is the required rate of return on Stock A? [4]

Ans: (a) 0.5; 0.4444; Stock B; (b) $E(R_p)$ 14.4%; σ_p 2.18%; (c) β_A 1.5; $E(R_A)$ 18.5%

cost of capital:

- cost of debt
- cost of preferred stock
- cost of common stock
- cost of retain earning

Debt

→ cost of debt after tax (K_{dt})

10 marks

Fixed

$$K_{dt} = K_d (1 - t)$$

where, K_d = cost of debt before tax
 t = tax.

$$K_d = \frac{I}{NP} \quad \text{if no maturity period}$$

 K_d = cost of debt I = interest NP = Net proceed (Actual received share or price)

ii if maturity period given.

$$K_d = \frac{I + \frac{M - NP}{n}}{\frac{M + 2NP}{3}}$$

where, M = Face value, par value, maturity value
 n = no. of years.

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$$K_{dt} = K_d (1 - t)$$

$$K_d t = K_d (1 - t)$$

Preference stock

$$K_{ps} = \frac{\text{Dps}}{NP} \quad \text{Dividend}$$

$$K_{ps} = \frac{Dps + \frac{M - NP}{n}}{\frac{M + 2NP}{3}}$$

cost of equity

→ Internal (Retained earnings) → External

$$(K_s) = \frac{D_1 + g}{P_0} \quad (K_e) = \frac{D_1}{NP} + g$$

D_1 = Expected Dividend / Next year Dividend

P_0 = stock current price

g = growth rate

$$D_1 = D_0 (1 + g)$$

D_0 = Last Year Dividend, just paid dividend

CAPM

cost of equity

$$K_s = R_f + (R_m - R_f) \times \beta$$

where,

R_f = Risk free rate

$R_m - R_f$ = market risk premium

β = Beta

Weighted Average cost of capital (WACC)

$$WACC = k_{dt} \times w_d + k_{ps} \times w_{ps} + k_s \times w_s + k_e \times w_e$$

2080 Q.No. 16

Sahara Company has the following capital structure, which it considers to be optimal:

| | |
|-----------------|------|
| Debt | 40% |
| Preferred stock | 10 |
| Common equity | 50 |
| | 100% |

Sahara's current dividend per share is Rs 30. Investors expect future earnings and dividends to grow at a constant rate of 5 percent per year forever. The company's stock currently sells for Rs 280 per share. New common stock can be sold for Rs 250 per share. Preferred stock can be sold with a dividend of Rs 14 to the public at a price of Rs 95 per share. Debt can be sold at an interest rate of 10 percent. Assume the applicable tax rate is 30 percent.

- Calculate the cost of each capital component.
- Calculate the weighted average cost of capital (WACC) assuming equity requirement is fulfilled from external equity only.
- What are the uses of cost of capital?

[6+3+1]

Ans: (a) $k_{dt} = 17.6\%$; $k_{ps} = 14.74\%$; $k_s = 16.25\%$; $k_e = 17.6\%$ (b) 12.399%

Given,

Weight of Debt (w_d) = 40% = 0.40

Weight of preferred stock (w_p) = 10% = 0.10

Weight of common equity (K_s) = 50% = 0.50

Current dividend (D_0) = Rs.30

Growth rate (g) = 5% = 0.05

Current selling price (P_0) = Rs.280 per share

New common stock (P_1) = Rs.250 per share

Dividend (DPS) = Rs.14

Price (NP) = Rs. 95 per share

Interest rate (K_d) = 10%

Tax rate (T) = 30% = 0.30

$$\begin{aligned} \text{a) Cost of Debt after tax (} K_{dt} \text{)} &= k_d(1-T) \\ &= 10\%(1-0.30) \\ &= 7\% \end{aligned}$$

$$\text{b) Cost of preferred stock (} K_{ps} \text{)} = D_pS / NP$$

$$= 14/95$$

$$= 14.73\%$$

c) Cost of Capital (K_s) = $D_1/P_0 + g$

$$= \frac{D_0(1+g)}{P_0} + 0.05$$

$$= \frac{30(1.05)}{280} + 0.05$$

$$= 16.25\%$$

d) Cost of equity (K_e) = $D_1/N_p + g$

$$= 31.5/250 + 0.05$$

$$= 17.6\%$$

Handwritten notes:

$$D_1 = D_0(1+g)$$

B) WACC = $W_d \cdot k_d + W_p \cdot K_{ps} + W_s \cdot K_e$

$$= 0.40 \cdot 17.6\% + 0.10 \cdot 14.73\% + 0.50 \cdot 17.6\%$$

$$=$$

2079 Q.No. 15 | 2064 Q.No. 8 | 2062 Q.No. 3

The small tool company was recently formed to manufacture a new product. The company has the following capital structure in the beginning of the year 2021.

| | |
|-----------------------------------------|-----------------------|
| 13% Debenture of 2030 | Rs. 6 million |
| 8% Preference stock | Rs. 2 million |
| Common stock (80,000 shares of Rs. 100) | Rs. 8 million |
| Total | Rs. 16 million |

The common stock sells for Rs. 200 a share on this date. Last year company paid dividend of Rs. 20 per share and expected to grow at the rate of 10 percent. The company has a marginal tax rate of 40 percent.

a. Compute the firm's weighted average cost of capital.

b. Is the figure computed in (a) is an appropriate acceptance criteria for evaluating new investment proposal? [8+2]

Ans: (a) 14.425% (b) Yes

Given,

Weight of debenture (W_d) = $6/16 = 0.375$

Weight of preference stock (W_p) = $2/16 = 0.125$

Weight of common stock (K_s) = $8/16 = 0.5$

Selling price for common stock (P_0) = Rs.200

Last year dividend (D_0) = Rs.20 per share

Growth rate (g) = 10%

Tax Rate (T) = 40% = 0.40

Interest rate (kd) = 13%

a) Requirement :

$$\begin{aligned} \text{WACC} &= W_d \cdot K_{dt} + W_p \cdot K_{ps} + W_s \cdot K_s \\ &= 0.375 \cdot 7.8\% + 0.125 \cdot 8\% + 0.5 \cdot 21\% \\ &= 14.425\% \end{aligned}$$

i) Cost of debt (K_{dt}) = $K_d(1-T)$
 $= 13\% (1-0.40)$
 $= 7.8\%$

ii) Cost of preferred stock (K_{ps}) = 8%

iii) Cost of common stock (K_s) = $D_1/P_0 + g$
 $= D_0(1+g)/P_0 + g$
 $= 20(1+0.10)/200 + 0.10$
 $= 0.21 \text{ or } 21\%$

$$\frac{D_1}{P_0} + g$$

B) yes it is an appropriate and acceptable criteria for evaluating new investment proposal because it has higher cost of common stock for return.

2078 Q.No. 15

Mega Company has the following capital structure, which it considers to be optimal:

| | |
|-----------------|-------------|
| Debt | 30% |
| Preferred stock | 20 |
| Common equity | <u>50</u> |
| | <u>100%</u> |

Mega's current dividend per share is Rs 15. Investors expect future earnings and dividends to grow at a constant rate of 6 percent per year forever. The company's stock currently sells for Rs 180 per share. New common stock can be sold for Rs 150 per share. Preferred stock can be sold with a dividend of Rs 12 to the public at a price of Rs 90 per share. Debt can be sold at an interest rate of 10 percent. Assume the applicable tax rate is 40 percent.

a. Calculate the cost of each capital component.

b. Calculate the weighted average cost of capital (WACC) assuming equity requirement is fulfilled from retained earning only. [6+4]

Ans: $k_{dt} = 6\%$; $k_s = 14.83\%$; $k_e = 16.6\%$; $k_{ps} = 13.33\%$ (b) 11.881%

7. 2075 Q.No. 16 | 2064 Q.No. 5 | 2063 Q.No. 7

The following table gives earnings per share figures for the Mega Trading Company during the preceding 5 years. The firm's common stock is now (1/1/2017) selling for Rs 70 per share, and the expected dividend at the end of the current year 2017 is 60 percent of the 2016 EPS. Because investors expect past trend to continue, g may be based on the earnings growth rate.

| Year | 2016 | 2015 | 2014 | 2013 | 2012 |
|------|------|------|------|------|------|
| EPS | 7.8 | 7.22 | 6.68 | 6.19 | 5.73 |

Current interest rate on new debt is 10 percent. The firm's marginal tax rate is 30 percent. The capital structure, considered to be optimal, is as follows:

| | |
|-------------------------------------|-----------------------|
| Debt | Rs 120 million |
| Common equity | Rs 180 million |
| Total liabilities and equity | Rs 300 million |

- Calculate company's after-tax cost of new debt and the cost of common equity assuming that new equity comes only from retained earnings.
- What is the company's weighted average cost of capital, again assuming that present capital structure is maintained?
- List out the important factors affecting the cost of capital.

[4+4+2]

Ans: (a) 7%; 14.71% (b) 11.625%

Given,

Selling price of common stock (P_0) = Rs.70 per share

Expected dividend (D_1) = 60% of 7.8
= Rs.4.68

$$\text{EPS 2016} = \text{EPS 2012} (1+g)^4$$

$$7.8 = 5.73 (1+g)^4$$

$$\text{Or, } 7.8/5.73 = (1+g)^4$$

$$\text{Or, } 1.36 = (1+g)^4$$

$$\text{Or, } 1.3613^{1/4} = (1+g)^{4 \times 1/4}$$

$$\text{Or, } 1.0802 = 1+g$$

$$\text{Or, } g = 0.0802 \text{ or } 8.0161\%$$

$$K_d = 10\%$$

$$\text{Cost of debt (Kdt)} = k_d(1-T)$$

$$= 10\%(1-30)$$

$$= 7\%$$

$$\text{Cost of equity (Ks)} = D_1/P_0 + g$$

$$= 4.68 / 70 + 0.0802$$

$$= 0.1471 \text{ or } 14.70\%$$

$$\text{Weight of debt (Wd)} = 120/300 = 0.4$$

$$\text{Weight of common stock (Ws)} = 180/300 = 0.6$$

$$\begin{aligned} \text{b) WACC} &= W_d \cdot K_{dt} + W_s \cdot K_s \\ &= 0.4 \cdot 7\% + 0.6 \cdot 14.70\% \\ &= 11.625\% \end{aligned}$$

Yes because it is higher than rate of return

$$2.36 \frac{1}{4} (1+g)^4$$

c) Important

Bond valuation

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Bond valuation :

| |
|-------------------------|
| value of bond today |
| Present value of bond |
| current value of bond |
| Intrinsic value of bond |

V_0

$V_0 = ?$

- Perpetual Bond • Zero coupon bond • Regular Bond

↓ No fixed Year ↓ No interest paid

$V_0 = I/k_d$ $V_0 = \frac{M}{(1+k_d)^n}$

Regular Bond (Impo) Given,

I = Interest (bond)

M = Par value / Face value / Maturity value → 1000

I = coupon rate, Interest paid by bond

i.e. coupon rate (C) = 12% $M = 1000$

$I = C \times 1000 = 12/100 \times 1000 = ?$

K_d = Market interest rate / Required rate of return / Going rate of return / Effective yield required

n = no. of Years maturity / maturity period

In case, After 2 Yrs, 3 Yrs

n = real Years - after Years

Regular Bond:

$$V_0 = I \times PVIFA_{kd\%, n \text{ yrs}} + M \times PVIF_{kd\%, n \text{ yrs}}$$

$I = \text{अंतर}$

$M = \text{मूल}$

$$I \times \left[\frac{1 - \frac{1}{(1+kd)^n}}{kd} \right] + \frac{M \times 1}{(1+kd)^n}$$

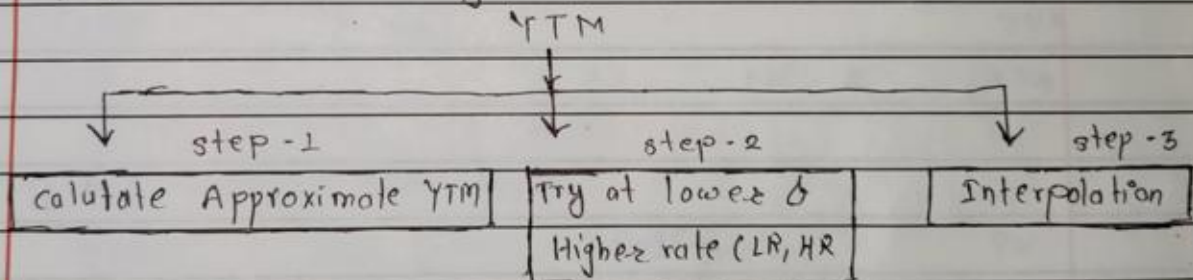
if semi-Annually

$n = \text{years} \times 2$, Interest rate $= I/2$, $kd = kd/2$

current yield $= I/V_0$

capital gain(loss) yield $= YTM - \text{current yield}$

Yield to maturity (YTM)



$$\text{Approximate YTM} = \frac{I + \frac{M - V_0}{n}}{\frac{M + 2V_0}{3}}$$

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e) Try at HR and LR

for example YTM = 5.67%

Try at 5% LR

Try at 6% HR

$$V_{LR} = I \times PVIFA_{kd\%, n/2} + M \times PVIF_{kd\%, n/2}$$

5%

$$V_{HR} = I \times PVIFA_{kd\%, n/2} + M \times PVIF_{kd\%, n/2}$$

6%

6%

3) By Interpolation

$$= \frac{V_{LR} - V_0}{V_{LR} - V_{HR}} \times (HR - LR)$$

$$V_{LR} - V_{HR}$$

$$\therefore V_0 = \text{Price of Bond}$$

2. 2080 Q.No. 15

Suppose Bagmati Textile Company sold an issue of bonds with a 10-year maturity, a Rs 1,000 par value, a 10 percent coupon rate, and annual interest payments.

a. If the investors required rate of return on such bonds is 12 percent. At what price would the bonds sell?

b. If actual price is Rs 900, calculate yield to maturity.

[4+6]

Ans: (a) Rs 887.02 (b) 11.76%

2078 Q.No. 14b

Given.

Number of maturity (n) = 10 years

Par value (M) = Rs.1000

Coupon interest © = 10%

Annual interest (I) = C*M or 10%*1000 = Rs.100

Require rate of return (KD) = 12%

V0?

$$V_0 = I \times PVIFA_{kd\%, n\text{year}} + M \times PVIF_{kd\%, n\text{year}}$$

$$= 100 \times PVIFA_{12\%, 10\text{years}} + 1000 \times PVIF_{12\%, 10\text{years}}$$

$$= 100 \times 5.6503 + 1000 \times 0.3220$$

$$= \text{Rs.}887.02$$

B: Given,

Price (P0) = Rs.900

Yield to maturity?

1st step:

Appropriate YTM =

$$I + \frac{M - V_0}{n}$$

$$\frac{M + 2V_0}{3}$$

$$150 + \frac{1000 - 887.02}{10}$$

$$1500 + 2 \times 887.02$$

$$\frac{111.298}{1258.0132}$$

3. 2078 Q.No. 14b

[4+6]

Ans: (a) Rs 887.02 (b) 11.75%

Suppose City Bank sold an issue of bonds with a 10-year maturity, a Rs 1,000 par value, a 12 percent coupon rate, and semi-annual interest payments. Market interest rate is 10 percent. Calculate value of bond at present. Would you purchase the bond if it is trading at Rs 1,050?

4. 2077 Q.No. 13

Ans: Rs. 1,124.63

Mega Bank has just issued bonds with an annual coupon rate of 8 percent, 7 years maturity and Rs 1,000 par value.

- If an investor required rate of return is 10 percent, how much can he/she pay for the bond at present? If bond is trading at Rs 900, would you suggest the investor to purchase the bond?
- How does value of the bond change with the change in market interest rate?

[7+3]

Ans: Rs 902.67

5. 2076 Q.No. 14a

5. 2076 Q.No. 14a

A company has Rs 1,000 par value, 14% coupon payment bond outstanding that has 15 years remaining until maturity. If investor's required rate of return is 12% what should be the price of bond today?

[5]

Ans: Rs 1,136.23

6. 2075 Q.No. 14

Suppose High-Tech Manufacturing Company sold an issue of bonds with a 10-year maturity, Rs 1,000 par value, a 10 percent coupon rate, and annual interest payments.

- Two years after the bonds were issued, the going rate of interest on bonds such as these fell to 8 percent. At what price would the bonds sell?
- Suppose that, 2 years after the initial offering, the going interest rate had risen to 12 percent. At what price would the bonds sell?
- Suppose that the conditions in part (a) existed that is, interest rates fall to 8 percent 2 years after the issue date. Suppose further that the interest rate remained at 8 percent for the next 10 years. Describe what would happen to the price of the company's bonds over time.

[4+4+2]

Ans: (a) Rs 1,114.96 (b) Rs 900.66

$$I = C \times M$$
$$n = 10$$
$$K_d = r$$
$$V_0 = I \times PVIFA_{K_d, n} + \frac{F}{(1 + K_d)^n}$$

$$V_0 = I \times PVIFA_{K_d, n} + \frac{F}{(1 + K_d)^n}$$

New Chapter Stock valuation – 12 marks

Formula:

Financial Assets valuation

(i) stock valuation:

⊗ calculation of value of stock at present under:

1. zero growth model

$$P_0 = \frac{D_0}{k_s}$$
2. constant growth model

$$P_0 = \frac{D_1}{k_s - g_c}$$
3. supernormal growth model

$$P_0 = \frac{D_1}{(1+k_s)^1} + \frac{D_2}{(1+k_s)^2} + \frac{D_3}{(1+k_s)^3} + \dots + \frac{D_n}{(1+k_s)^n} + \frac{P_n}{(1+k_s)^n}$$

$$\begin{aligned}
 D_1 &= D_0(1+g) = \\
 D_2 &= D_1(1+g) = \\
 D_3 &= D_2(1+g) = \\
 D_4 &= D_3(1+g) = \\
 D_5 &= D_4(1+g) = \\
 D_6 &= D_5(1+g) =
 \end{aligned}$$

$$\begin{aligned}
 P_1 &= \frac{D_2}{(1+k_s)^1} + \frac{D_3}{(1+k_s)^2} + \frac{D_4}{(1+k_s)^3} + \frac{D_5}{(1+k_s)^4} + \frac{D_6}{(1+k_s)^5} + \frac{P_6}{(1+k_s)^5} \\
 P_2 &= \frac{D_3}{(1+k_s)^1} + \frac{D_4}{(1+k_s)^2} + \frac{D_5}{(1+k_s)^3} + \frac{D_6}{(1+k_s)^4} + \frac{P_6}{(1+k_s)^4} \\
 P_3 &= \frac{D_4}{(1+k_s)^1} + \frac{D_5}{(1+k_s)^2} + \frac{D_6}{(1+k_s)^3} + \frac{P_6}{(1+k_s)^3} \\
 P_4 &= \frac{D_5}{(1+k_s)^1} + \frac{D_6}{(1+k_s)^2} + \frac{P_6}{(1+k_s)^2}
 \end{aligned}$$

Descriptive Answer Questions

2080 Q.No. 14
 Janakpur Sweets Company is experiencing a period of rapid growth. Earnings and dividends are expected to grow at a rate of 10 percent during the next 2 years, at 8 percent in the third year, and at 5 percent constant rate thereafter. Company's last dividend was Rs 20 and the required rate of return on the stock is 15 percent.

- Calculate the value of the stock today.
- Calculate value of stock at the end of year 1, (P_1).
- Calculate the dividend yield and capital gain yield for the first year.

[4+3+3]
 Ans: (a) Rs 274.428 (b) Rs 248.31 (c) 5.64%

2079 Q.No. 14
 Everest Company's current stock price is Rs. 360 and its last dividend was Rs. 24. In view of company's strong financial position and its consequent low risk, its required rate of return is only 12 percent. If dividends are expected to grow at a constant rate in the future, and if required rate of return on stock is expected to remain 12 percent, what is company's expected stock price 5 years from now?

[10]
 Ans: $g = 5\%$; Rs 459.46

$$\begin{aligned}
 g_{1-2} &= \\
 g_3 &= \\
 g &=
 \end{aligned}$$

$$P_0 = \frac{D_1}{(1+k_s)^1} + \frac{D_2}{(1+k_s)^2} + \frac{D_3}{(1+k_s)^3} + \frac{P_3}{(1+k_s)^3}$$

$$\begin{aligned}D1 &= D0(1+g) \\&= 20(1+.10) = 22 \\D2 &= D1(1+g) \\&= 22(1+.10) = 24.20 \\D3 &= D2(1+g) \\&= 24.20(1+0.08) = 26.14 \\D4 &= D3(1+g) \\&= 26.14(1+0.05) = 27.45 \\P3 &= D4\end{aligned}$$

Chapter 9: Working Capital Management 2 marks